

Engin II Exam I Review

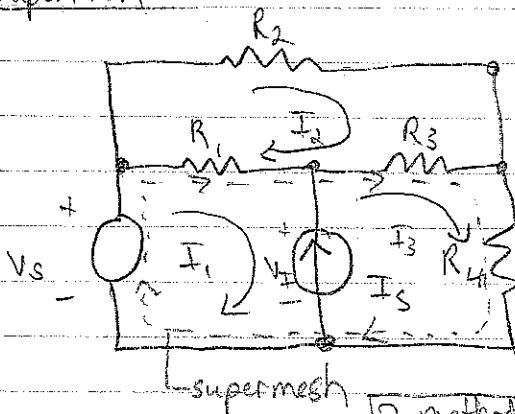
Ch.1-4 Topics to know:

- $V \div$
- $I \div$
- Ohm's Law
- KVL
- KCL
- Supermesh/Supernode
- Thevenin/Norton
- R in series & parallel
- Source Transformation
- Max Power Transfer Thm.
- Superposition
- Dependent Sources

Will be given: (if asked)

- Δ -Y or Y- Δ

Supermesh



Find power dissipated across R_4 (P_{R4})

- ① $V_s - (I_1 - I_2)R_1 - V_I = 0$
- ② $-R_2 I_2 - R_3 (I_2 - I_3) - R_1 (I_2 - I_1) = 0$
- ③ $-R_3 (I_3 - I_2) - R_4 I_3 + V_I = 0$
- ④ $I_3 - I_1 = I_s$

2 methods to solve

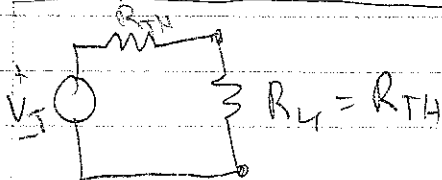
$$\sum_{\text{supermesh loop}} V = V_s - R_1 (I_1 - I_2) - R_3 (I_3 - I_2) - R_4 (I_3) = 0$$

$$\sum_{\text{loop 2}} V = 0 = -R_2 I_2 - R_3 (I_2 - I_3) - R_1 (I_2 - I_1)$$

Supermesh equation: $I_3 - I_1 = I_s$

$$P_{R4} = R_4 I_3^2$$

Max. power delivered to R_4



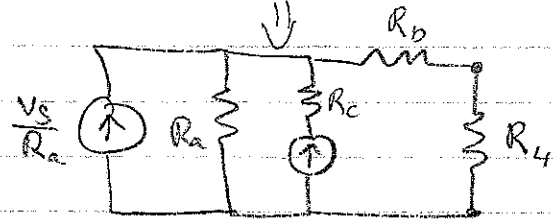
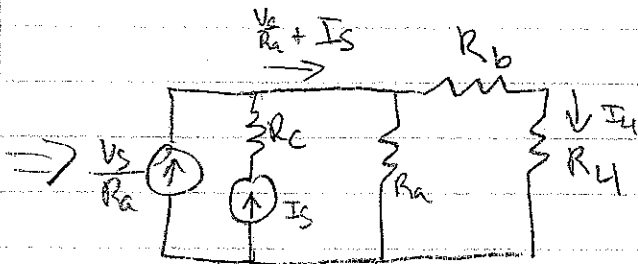
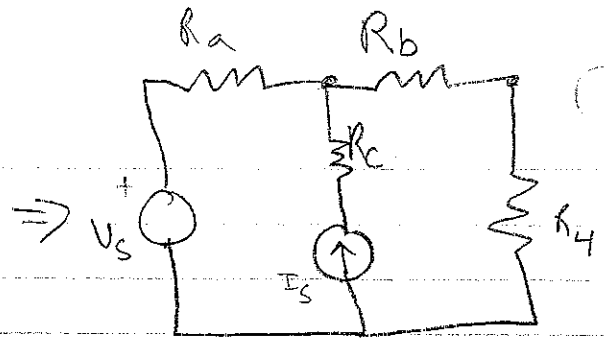
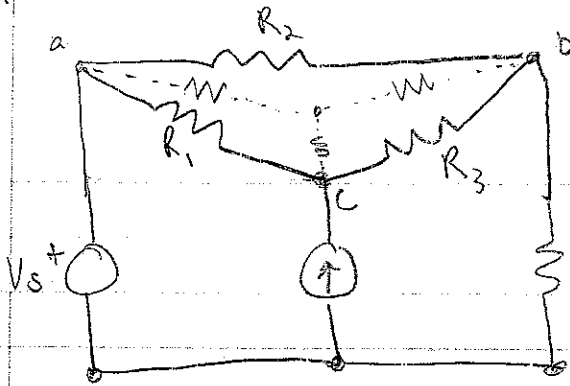
Note: If: Then:

$V_s \rightarrow 0 \Rightarrow$ S.C.

$I_s \rightarrow 0 \Rightarrow$ O.L.

can't "look in" to a circuit to find R_{TH} if there are dependent sources

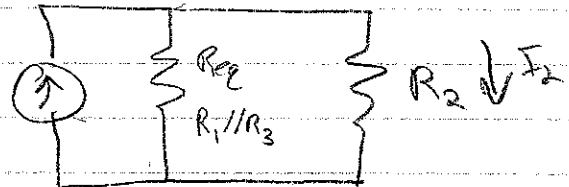
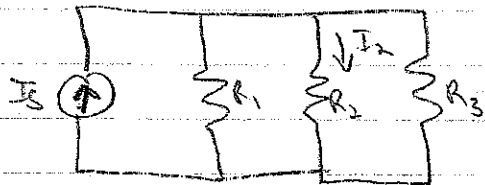
$\Delta \rightarrow Y$



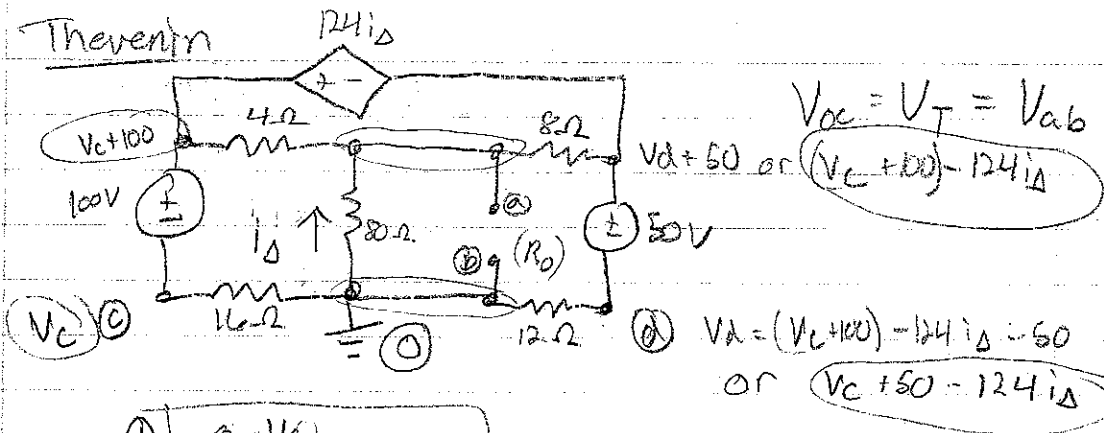
Don't need to worry about R_c , we want to know about R_4

Can find I_4 w/ current ÷

Current divider



Thevenin



$$\textcircled{1} \frac{0 - V_a}{80} = i_{\Delta}$$

Unknown: V_a, V_c, i_{Δ}

$$\textcircled{2} \sum_a i = 0 = \frac{V_C + 100 - V_a}{4} - \frac{V_a}{80} - \left[V_a \left\{ (V_C + 100) - 124 \left(\frac{-V_a}{80} \right) \right\} \right]$$

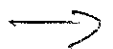
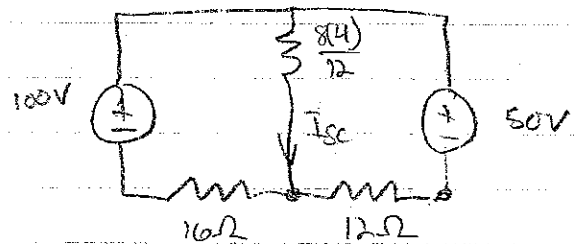
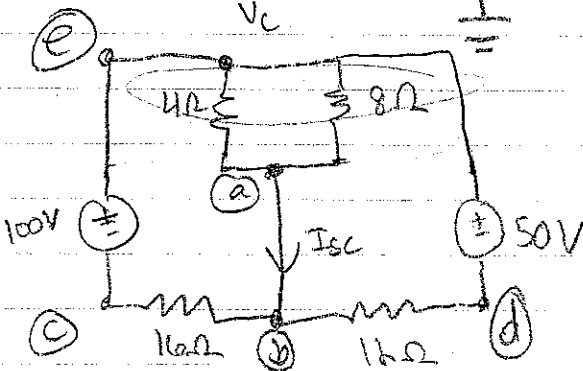
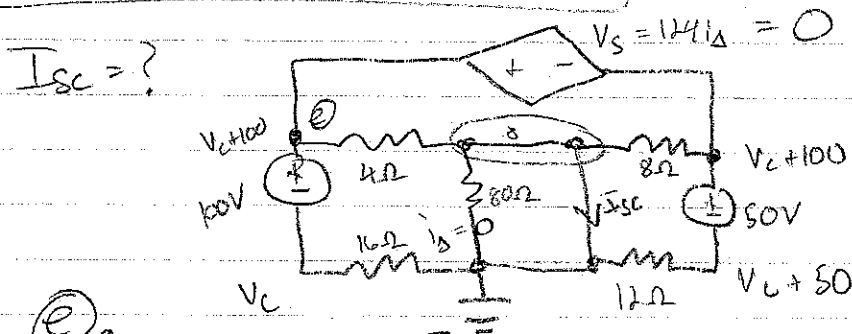
$$\textcircled{3} \sum_b i = 0 = \frac{V_C}{16} + \frac{V_a}{80} + \frac{V_C + 50 - 124 \left(\frac{-V_a}{80} \right)}{12}$$

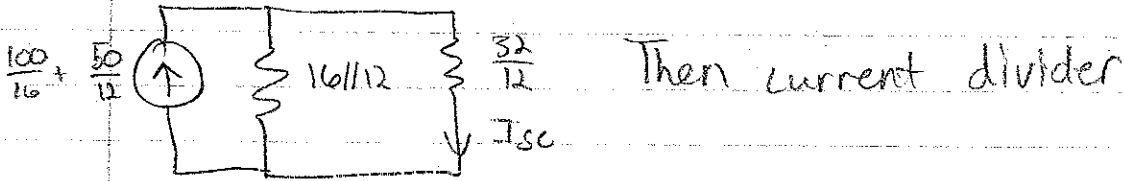
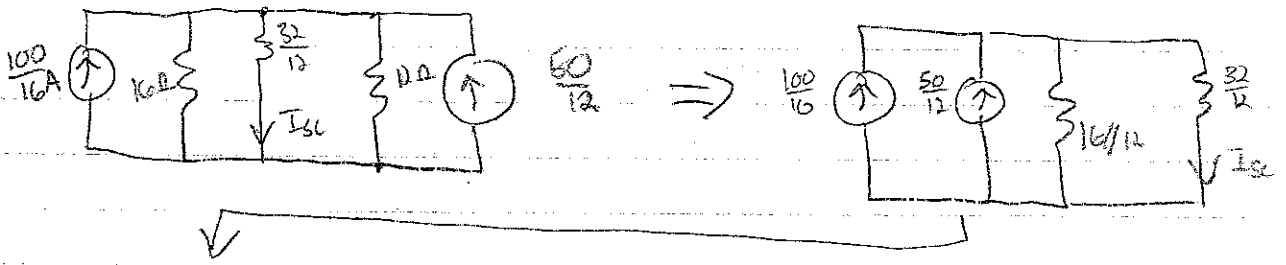
Leq, 2 unk. $V_a = ? = V_{oc} = V_T$

$$V_{oc} = V_T \quad R_{Th} = \frac{V_{oc}}{I_{sc}}$$

$$I_{sc} = I_N$$

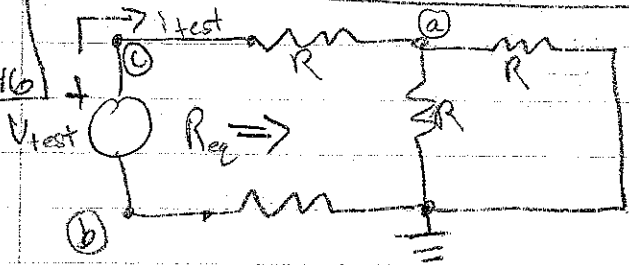
$I_{sc} = ?$





$$R_0 = R_T = \frac{V_T}{I_{sc}} = R \text{ for max power transfer}$$

Alternate method from pg. 146



Apply V_{test} to find i_{test}

$$\text{Then } R_{eq} = \frac{V_{test}}{I_{test}}$$

$$\sum_a i = \frac{V_b + V_{test} - V_a}{R} - \frac{2V_a}{R} = 0$$

$$\sum_{\text{ground}} i = \frac{2V_a}{R} + \frac{V_b}{R} = 0$$

$$V_b = -2V_a$$

$$\sum_a i = -3V_a + V_{test} - 2V_a = 0$$

$$V_a = \frac{V_{test}}{5}$$

$$V_c = -2V_a + V_{test} = \left(-\frac{2}{5} + 1\right)V_{test} = \frac{3}{5}V_{test}$$

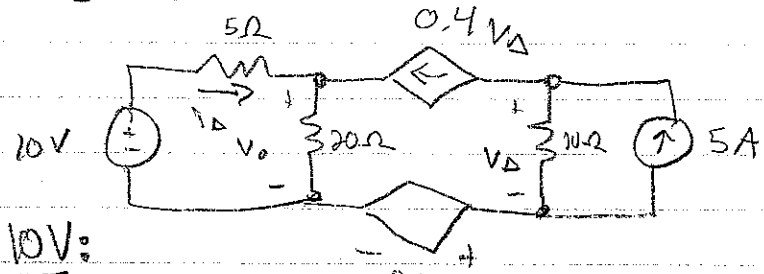
$$I_{test} = \frac{\frac{3}{5}V_{test} - \frac{1}{5}V_{test}}{R} = \frac{2V_{test}}{5R}$$

$$R_{eq} = \frac{V_{test}}{\frac{2V_{test}}{5R}} = \frac{5}{2}R$$

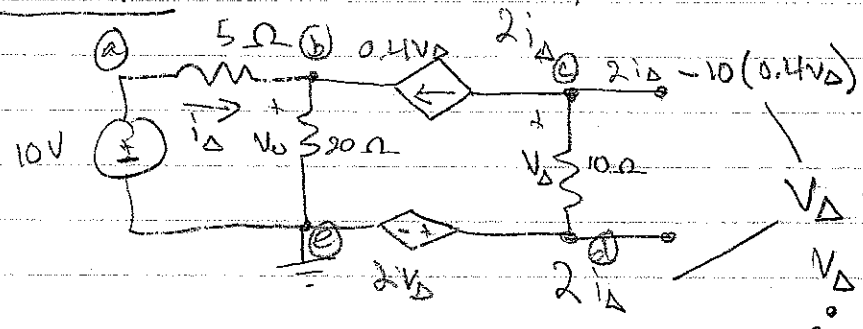
check:



Ex. 4.13 pg 154



From 10V:



$$V_{\Delta} = V_c - V_d = \frac{2i_{\Delta} - 4V_{\Delta} - 2i_{\Delta}}{10}$$

$$V_{\Delta} = -0.4V_{\Delta}$$

$$\therefore V_{\Delta} = 0$$

$$\text{and } v_o = \frac{20}{25}(10) = 8V$$